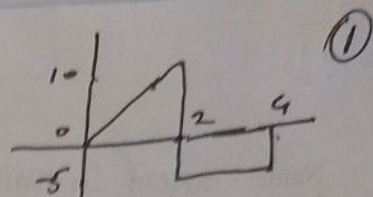


| | | | |
|-----|-------------|----------------|----------|
| | $= 0$ | $t < 0$ | gradient |
| (1) | $f(t) = 5t$ | $0 \leq t < 2$ | $m = 5$ |
| | $= -5$ | $2 \leq t < 4$ | $m = 5$ |
| | $= 0$ | $t \geq 4$ | |



(a) From $0 \leq t < 2$

$$f(t) = 5t u(t) - 5(t-2)u(t-2)$$

At 2

There is a jump down from 10 to -5

Therefore there is unit step $-15u(t-2)$

At $t=4$ it jumps back up to '0'. So

$$+ 5u(t-4)$$

$$\therefore f(t) = 5t u(t) - 5(t-2)u(t-2) - 15u(t-2) + 5u(t-4)$$

(b) $F(s) = \mathcal{L}[f(t)]$

$$= \mathcal{L}(5t u(t) - 5(t-2)u(t-2) - 15u(t-2) + 5u(t-4))$$

$$= \frac{5}{s^2} - \frac{5}{s^2} e^{-2s} - \frac{15}{s} e^{-2s} + \frac{5}{s} e^{-4s}$$

(2)

$$(2) \quad \frac{2s+1}{s^2+4}$$

(a) Find initial value of $v(t)$, $v(0^+)$

(i) $v(0^+) = \lim_{s \rightarrow \infty} (V(s)) s$ — 7.36 in the Book.

$$v(0^+) = \lim_{s \rightarrow \infty} \left[\frac{2s+1}{s^2+4} \right] s$$

$$= \lim_{s \rightarrow \infty} \left[\frac{2 + 1/s}{1 + 4/s} \right] \frac{s}{s}$$

$$= \frac{2+0}{1+0}$$

$$v(0^+) = 2.$$

$$(ii) \quad \begin{aligned} V(s) &= \frac{2s+1}{s^2+4} \\ &= \frac{2s}{s^2+4} + \frac{1}{s^2+4} \end{aligned}$$

$$V(s) = 2 \left[\frac{s}{s^2+2^2} \right] + \frac{1}{2} \left[\frac{2}{s^2+2^2} \right]$$

$$\mathcal{L}^{-1}(V(s)) = v(t)$$

$$v(t) = \left[2 \cos 2t + \frac{1}{2} \sin 2t \right] u(t)$$

From Table

7.2. (8 & 9)

$v(t)$ $F(s)$

$\sin(bt)$ $\frac{b}{s^2+b^2}$

$\cos bt$ $\frac{s}{s^2+b^2}$

For $R(s) > 0$.

$$\begin{aligned}
 v(0^+) &= 2 \cos(0) + \frac{1}{2} \sin 0. \\
 &= 2(1) + \frac{1}{2}(0) \\
 &= 2.
 \end{aligned}$$

(3)

Same as a(i)

(b) Find Final value of $v(t)$,

(i) $\lim_{t \rightarrow \infty} v(t) = \lim_{s \rightarrow 0} s F(s)$ — 7.39 in Book.

$$\begin{aligned}
 \therefore v(\infty) &= \lim_{s \rightarrow 0} \left(\frac{2s^2 + s}{s^2 + 4} \right) \\
 &= \frac{0 + 0}{0 + 4}
 \end{aligned}$$

$$v(\infty) = 0$$

(ii) $v(t) = \left[2 \cos(2t) + \frac{1}{2} \sin 2t \right] u(t)$ from a(ii)

~~Exa~~ This is a non-ending ^{periodic/oscillating} signal $v(\infty)$ does not exist.

The above final-value property 7.39 in b(i) is incorrect. It requires for signal $v(t)$ to give a final value. If the signal does not have a final value, then this property is not valid. BOOK page 358

(3)

(4)

$$(a) F(s) = \frac{e^{-2s}}{s(s+1)} = e^{-2s} \left[\frac{1}{s(s+1)} \right]$$

Partial Fractions for expression inside the brackets

$$\frac{1}{s(s+1)} = \left[\frac{A}{s} + \frac{B}{s+1} \right]$$

~~$$\frac{1}{s(s+1)} = \frac{(s+1)A + sB}{s(s+1)}$$~~

$$\Rightarrow (s+1)A + sB = 1$$

For $s=0$.

$$A = 1$$

For $s=-1$

$$B = -1$$

$$\therefore F(s) = e^{-2s} \left[\frac{1}{s} - \frac{1}{s+1} \right]$$

$$\mathcal{L}^{-1}[F(s)] = e^{-2s} \mathcal{L}^{-1}\left[\frac{1}{s}\right] - e^{-2s} \mathcal{L}^{-1}\left[\frac{1}{s+1}\right]$$

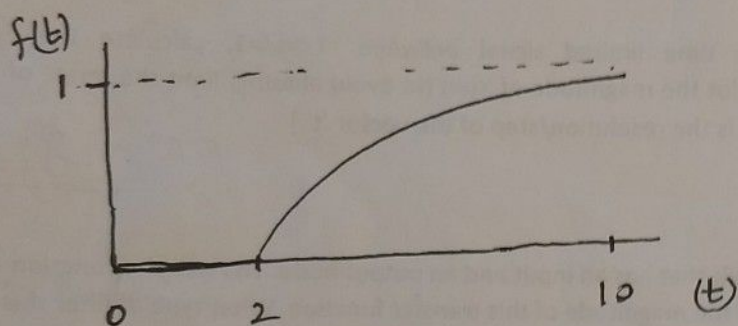
$$= u(t-2) - e^{-(t-2)} u(t-2)$$

$$= [1 - e^{-(t-2)}] u(t-2)$$

(5)



Plot

before $(t-2)$ $f(t)$ is 0for $t=2$ $f(t) = 0$.for $t=10$ $f(t) = 0.9997$.

$$(b) \quad F(s) = \frac{1 - e^{-s}}{s(s+1)}$$

From Partial Fractions in (a)

$$F(s) = (1 - e^{-s}) \left[\frac{1}{s} - \frac{1}{s+1} \right]$$

$$F(s) = \left[\frac{1}{s} - \frac{1}{s+1} \right] - e^{-s} \left[\frac{1}{s} - \frac{1}{s+1} \right]$$

$$\mathcal{L}^{-1}[F(s)] = \mathcal{L}^{-1}\left[\frac{1}{s}\right] - \mathcal{L}^{-1}\left[\frac{1}{s+1}\right] - e^{-s} \mathcal{L}^{-1}\left[\frac{1}{s}\right] + e^{-s} \mathcal{L}^{-1}\left[\frac{1}{s+1}\right]$$

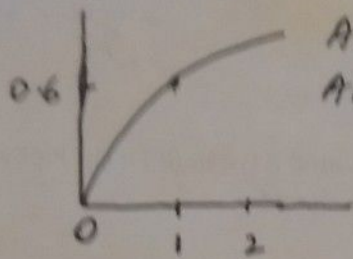
$$= u(t) - e^{-t} u(t) - u(t-1) + e^{-(t-1)} u(t-1)$$

$$= (1 - e^{-t}) u(t) - (1 - e^{-(t-1)}) u(t-1)$$

Plot

(6)

$$f_1(t) = 1 - e^{-t} u(t) \quad \text{At } t=0, 0.$$

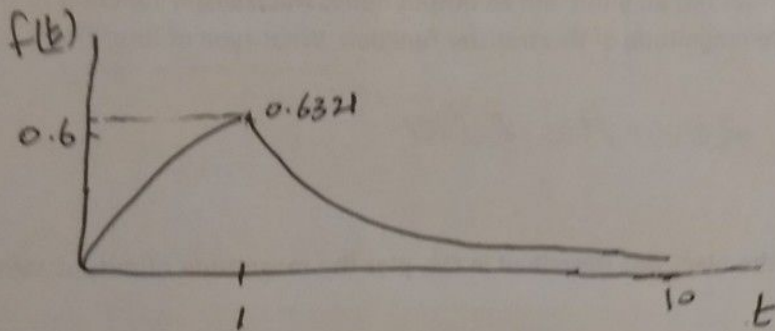


$$\text{At } t=1, 0.6321$$

$$\text{At } t=10, \approx 1$$

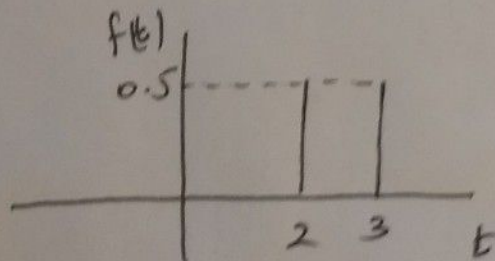
$$f_2(t) = -(1 - e^{-(t-1)}) u(t-1)$$

$$\text{At } t=1 \quad f_2(t) = 0$$



$$(c) \quad F(s) = \frac{e^{-2s} - e^{-3s}}{2}$$

$$\begin{aligned} \mathcal{L}^{-1} F(s) &= \frac{1}{2} \mathcal{L}^{-1}[e^{-2s}] - \frac{1}{2} \mathcal{L}^{-1}[e^{-3s}] \\ &= \frac{1}{2} (\delta(t-2) - \delta(t-3)) \end{aligned}$$



$$(d) F(s) = \frac{1 - e^{-5s}}{s(s+5)} = 1 - e^{-5s} \left[\frac{1}{s(s+5)} \right] \quad (7)$$

Partial Fraction for expression inside the brackets

$$\frac{1}{s(s+5)} = \frac{A}{s} + \frac{B}{s+5}$$

$$1 = A(s+5) + Bs$$

for $s=0$.

$$A = \frac{1}{5}$$

For $s=-5$.

$$B = -\frac{1}{5}$$

$$\therefore F(s) = (1 - e^{-5s}) \left[\frac{1}{5s} - \frac{1}{5(s+5)} \right]$$

$$F(s) = \left[\frac{1}{5s} - \frac{1}{5(s+5)} \right] - e^{-5s} \left[\frac{1}{5s} - \frac{1}{5(s+5)} \right]$$

$$\mathcal{L}^{-1}[F(s)] = \mathcal{L}^{-1}\left(\frac{1}{5s}\right) - \mathcal{L}^{-1}\left[\frac{1}{5(s+5)}\right] - e^{-5s} \mathcal{L}^{-1}\left[\frac{1}{5s}\right] + e^{-5s} \mathcal{L}^{-1}\left[\frac{1}{5(s+5)}\right]$$

$$= \frac{u(t)}{5} - \frac{e^{-5t} u(t)}{5} - \frac{u(t-5)}{5} + e^{-5(t-5)} u(t-5)$$

$$= \frac{1}{5} \left[(1 - e^{-5t}) u(t) - (1 - e^{-5(t-5)}) u(t-5) \right]$$

(8)

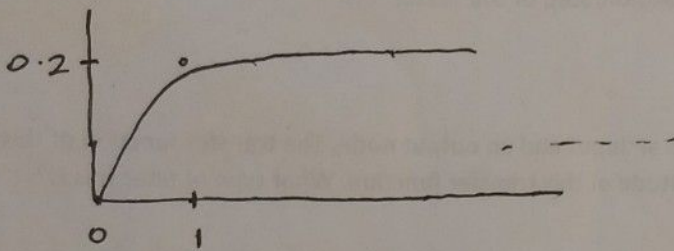
Plot.

$$f_1(t) = \frac{1}{5} (1 - e^{-5t})$$

$$\text{At } t=0, 0.$$

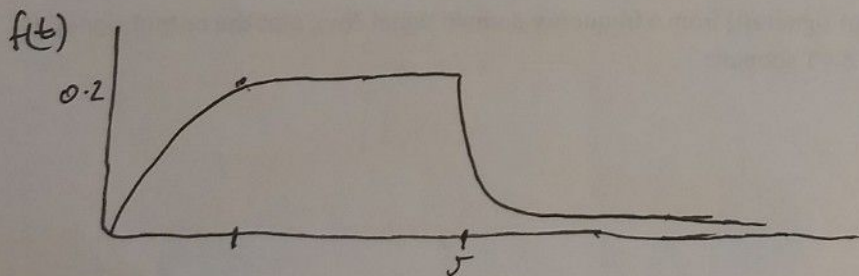
$$t=1, 0.99/5 \approx 0.2$$

$$t=2, \approx 1 \approx 0.2.$$



$$f_2(t) = -\frac{1}{5} (1 - e^{-5(t-5)}) u(t-5).$$

$$\text{At } t=5, f_2(t) \approx 0$$



(4)

(9)

$$(i) \frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 4 y(t) = 2 x(t)$$

(a) impulse response.

$$s^2 Y(s) + 5s Y(s) + 4Y(s) = 2X(s)$$

For impulse response $X(s) = 1$

$$H(s) = \frac{Y(s)}{X(s)} = \frac{2}{s^2 + 5s + 4}$$

$$= \frac{2}{s^2 + 4s + 1s + 4}$$

$$= \frac{2}{(s+4)(s+1)}$$

Partial Fractions.

$$\frac{2}{(s+4)(s+1)} = \frac{2A}{s+4} + \frac{2B}{s+1}$$

$$2 = 2A(s+1) + 2B(s+4)$$

$$s = -1$$

$$2 = 2B(3)$$

$$B = \frac{1}{3}$$

$$s = -4$$

$$2 = 2A(-3)$$

$$A = -\frac{1}{3}$$

$$H(s) = \frac{2}{3} \left(\frac{-1}{(s+4)} + \frac{1}{(s+1)} \right)$$

$$\mathcal{L}^{-1}[H(s)] = \frac{2}{3} \left(\mathcal{L}^{-1} \left[\frac{1}{s+1} \right] - \mathcal{L}^{-1} \left[\frac{1}{s+4} \right] \right)$$

$$h(t) = \frac{2}{3} (e^{-t} - e^{-4t})$$

(b) $\frac{d^2 y(t)}{dt^2} + 5 \frac{dy(t)}{dt} + 4y(t) = 2x(t)$

For unit step $x(t) = u(t)$

$$\& \mathcal{L} u(t) = \frac{1}{s}$$

$$\therefore X(s) = \frac{1}{s}$$

From (a)

$$S(s) = \frac{Y(s)}{X(s)} = \frac{2}{s^2 + 5s + 4}$$

$$S(s) = sY(s) = \frac{2}{(s+4)(s+1)}$$

$$S(s) = \frac{2}{s(s+1)(s+4)}$$

Partial Fractions.

$$\frac{2}{s(s+1)(s+4)} \equiv \frac{2A}{s} + \frac{2B}{s+1} + \frac{2C}{s+4}$$

(11)

$$2 = 2A(s+1)(s+4) + 2Bs(s+4) + 2Cs(s+1)$$

For $s=0$

$$2 = 2A(1)(4)$$

$$A = \frac{1}{4}$$

For $s=-1$

$$2 = 2B(-1)(3)$$

$$B = -\frac{1}{3}$$

For $s=-4$

$$2 = 2C(-4)(-3)$$

$$C = \frac{1}{12}$$

$$S(s) = \frac{1}{2s} - \frac{2}{3(s+1)} + \frac{1}{6(s+4)}$$

$$\mathcal{L}^{-1} S(s) = \frac{1}{2} \mathcal{L}^{-1} \left[\frac{1}{s} \right] - \frac{2}{3} \mathcal{L}^{-1} \left[\frac{1}{s+1} \right] + \frac{1}{6} \mathcal{L}^{-1} \left[\frac{1}{s+4} \right]$$

$$s(t) = \left[\frac{1}{2} - \frac{2}{3} e^{-t} + \frac{1}{6} e^{-4t} \right] u(t)$$

(12)

$$(c) \quad h(t) = \frac{d s(t)}{dt}$$

$$\frac{d s(t)}{dt} = \frac{d}{dt} \left[\frac{1}{2} - \frac{2e^{-t}}{3} + \frac{1}{6}e^{-4t} \right]$$

$$= \frac{2e^{-t}}{3} - \frac{4e^{-4t}}{6}$$

$$\frac{d s(t)}{dt} = \frac{2}{3} (e^{-t} - e^{-4t}) = h(t)$$

Hence Verified.

$$(ii) \quad \frac{d^2}{dt^2} y(t) + 5 \frac{dy(t)}{dt} + 4 y(t) = 2 \frac{dx(t)}{dt} + 6 x(t)$$

(a) impulse Response

$$s^2 Y(s) + 5s Y(s) + 4 Y(s) = 2sX(s) + 6X(s)$$

$$H(s) = \frac{Y(s)}{X(s)} = \frac{(2s+6)}{(s^2+5s+4)}$$

$$= \frac{2s+6}{(s+1)(s+4)}$$

$$(2s+6) = A(s+4) + B(s+1)$$

(13)

$$s = -4.$$

$$-8 + 6 = -3B.$$

$$B = \frac{2}{3}.$$

$$s = -1$$

$$4 = 3A$$

$$A = \frac{4}{3}.$$

$$H(s) = \frac{4/3}{s+1} + \frac{2/3}{(s+4)}$$

$$h(t) = \mathcal{L}^{-1}\{H(s)\} = \frac{4}{3}e^{-t} + \frac{2}{3}e^{-4t}.$$

$$h(t) = \frac{2}{3} (2e^{-t} + e^{-4t})$$

$$(b) \quad S(s) = sY(s) = \frac{2s+6}{(s+1)(s+4)}$$

$$S(s) = Y(s) = \frac{2s+6}{s(s+1)(s+4)}$$

$$\frac{2s+6}{(s+1)(s+4)} = \frac{A}{s} + \frac{B}{(s+1)} + \frac{C}{s+4}$$

$$(ii) \frac{d^3 y(t)}{dt^3} + 3 \frac{d^2 y(t)}{dt^2} + 4 \frac{dy(t)}{dt} + 2 y(t) = 6 x(t).$$

$$(a) s^3 Y(s) + 3s^2 Y(s) + 4s Y(s) + 2 Y(s) = 6 X(s).$$

$$\frac{Y(s)}{X(s)} = \frac{6}{s^3 + 3s^2 + 4s + 2}$$

$$H(s) = \frac{6}{(s+1)(s+1+j)(s+1-j)}$$

$$H(s) = \frac{A}{(s+1)} + \frac{B}{(s+1+j)} + \frac{C}{(s+1-j)}$$

$$6 = A(s+1+j)(s+1-j) + B(s+1)(s+1-j) + C(s+1)(s+1+j)$$

$$s = -1.$$

$$A(-1+1+j)(-1+1-j) = 6$$

$$A = +6.$$

$$s = -1-j$$

$$B(-1+1-j)(-1+1-j-j) = 6.$$

$$B(-j)(-2j) = 6.$$

$$B = \frac{6}{2j^2} = -3$$

$$s = -1+j$$

$$C(j)(2j) = 6 \Rightarrow C = -3$$

$$2s+6 = A(s+1)(s+4) + Bs(s+4) + Cs(s+1)$$

$$s = 0$$

$$6 = A(1)(4).$$

$$A = \frac{3}{2}.$$

$$s = -1$$

$$4 = B(-1)(+3).$$

$$B = -\frac{4}{3}$$

$$s = -4.$$

$$-2 = C(-4)(-3).$$

$$C = -\frac{1}{6}.$$

$$S(s) = \frac{3}{2s} - \frac{4}{3(s+1)} - \frac{1}{6(s+4)}$$

$$L^{-1}[S(s)] = \left[\frac{3}{2} - \frac{4}{3}e^{-t} - \frac{1}{6}e^{-4t} \right] u(t).$$

$$(c) \frac{d s(t)}{dt} = \frac{d}{dt} \left[\frac{3}{2} \right] - \frac{4}{3} \frac{d}{dt} e^{-t} - \frac{1}{6} \frac{d}{dt} e^{-4t}$$

$$\boxed{\frac{d s(t)}{dt} = \frac{4}{3}e^{-t} + \frac{2}{3}e^{-4t} = h(t)}$$

$$(ii) \frac{d^3}{dt^3} y(t) + 3 \frac{d^2}{dt^2} y(t) + 4 \frac{d}{dt} y(t) + 2 y(t) = 6 x(t).$$

$$(a) s^3 Y(s) + 3s^2 Y(s) + 4s Y(s) + 2 Y(s) = 6 X(s).$$

$$\frac{Y(s)}{X(s)} = \frac{6}{s^3 + 3s^2 + 4s + 2}$$

$$H(s) = \frac{6}{(s+1)(s+1+j)(s+1-j)}$$

$$H(s) = \frac{A}{(s+1)} + \frac{B}{(s+1+j)} + \frac{C}{(s+1-j)}$$

$$6 = A(s+1+j)(s+1-j) + B(s+1)(s+1-j) + C(s+1)(s+1+j)$$

$$s = -1.$$

$$A(-1+1+j)(-1+1-j) = 6$$

$$A = +6.$$

$$s = -1-j$$

$$B(-1+1-j)(-1+1-j-j) = 6.$$

$$B(-j)(-2j) = 6.$$

$$B = \frac{6}{2j^2} = -3$$

$$s = -1+j$$

$$C(j)(2j) = 6 \Rightarrow C = -3$$

$$H(s) = \frac{6}{(s+1)} - \frac{3}{(s+1+j)} - \frac{3}{(s+1-j)} \quad (16)$$

$$\begin{aligned} \mathcal{L}^{-1}[H(s)] &= 6e^{-t} - 3e^{(-1-j)t} - 3e^{(-1+j)t} \\ &= 6e^{-t} - 3e^{-t} (e^{-jt} + e^{jt}) \times 2 \end{aligned}$$

$$h(t) = 6e^{-t} - 6e^{-t} \cos t$$

$$(b) \quad S(s) = \frac{6}{s(s+1)(s^2+2s+2)}$$

$$S(s) = \frac{A}{s} + \frac{B}{s+1} + \frac{Cs+D}{s^2+2s+2}$$

$$6 = A(s+1)(s^2+2s+2) + B(s)(s^2+2s+2) + (Cs+D)(s)(s+1)$$

$$s=0$$

$$6 = A(1)(2)$$

$$A=3$$

$$s=-1$$

$$B(-1)(1-2+2) = 6$$

$$B = -6$$

$$s=1$$

$$6 = 3(2)(5) - 6(1)(5) + Cs+D(2)$$

$$3 = 30 - 30 + C+D$$

$$C = 3 - D \quad \text{--- (1)}$$

$$s=2$$

$$6 = 3 \times 3 \times 10 + 6 \times 2 \times 10 + 6(2C+D)$$

$$6(2C+D) + 90 - 120 = 6$$

$$6(2C+D) = 36$$

$$2C+D = 6$$

$$\text{Put (1)}$$

$$6 - 2D + D = 6 \Rightarrow D = 0$$

$$C = 3$$

$$\therefore S(s) = \frac{3}{s} - \frac{6}{s+1} + \frac{3s}{(s+1)^2+1}$$

$$= \frac{3}{s} - \frac{6}{s+1} + \frac{3(s+1) - 3}{(s+1)^2+1}$$

$$S(s) = \frac{3}{s} - \frac{6}{s+1} + \frac{3(s+1)}{(s+1)^2+1} - \frac{3(1)}{(s+1)^2+1} \quad (17)$$

$$s(t) = \mathcal{L}^{-1}\left(3 - 6e^{-t} + 3e^{-t}\cos t - 3e^{-t}\sin t\right)$$

$$(c) \quad \frac{d}{dt} s(t) = 6e^{-t} - 3e^{-t}\cos t - 3e^{-t}\sin t + 3e^{-t}\sin t - 3e^{-t}\cos t$$

$$\frac{d}{dt} s(t) = 6e^{-t} - 6e^{-t}\cos t = h t$$

Hence verified

$$(iv) \frac{d^3 y(t)}{dt^3} - \frac{d^2 y(t)}{dt^2} + 2y(t) = 4 \frac{dx(t)}{dt} - 8x(t)$$

Impulse Response

$$(a) s^3 Y(s) - s^2 Y(s) + 2Y(s) = 4sX(s) - 8X(s)$$

$$\frac{Y(s)}{X(s)} = \frac{4s-8}{s^3-s^2+2}$$

$$H(s) = \frac{4s-8}{(s+1)(s^2-2s+2)}$$

$$H(s) = \frac{A}{s+1} + \frac{Bs+C}{(s^2-2s+2)}$$

$$4s-8 = A(s^2-2s+2) + (Bs+C)(s+1)$$

$$s = -1$$

$$-4-8 = A(1+2+2)$$

$$\frac{-12}{5} = A$$

$$s = 0$$

$$-8 = \frac{-24}{5} + C$$

$$\frac{24-40}{5} = C$$

$$C = \frac{-16}{5}$$

$$s = 1$$

$$4-8 = \frac{-12}{5} + 2B + 2C$$

$$-4 + \frac{12}{5} - 2C = 2B$$

$$\frac{-20+12+32}{10} = B$$

$$B = \frac{24}{10} = \frac{12}{5}$$

$$\therefore H(s) = \frac{-12}{5(s+1)} + \frac{(\frac{12s-16}{5})}{(s^2-1)+1}$$

$$H(s) = \frac{-12}{s(s+1)} + \frac{12}{5} \frac{s}{(s-1)^2+1} - \frac{16/5}{(s-1)^2+1}$$

$$= \frac{-12}{s(s+1)} + \frac{12}{5} \frac{[(s-1)+1]}{(s-1)^2+1} - \frac{16/5}{(s-1)^2+1}$$

$$H(s) = \frac{-12}{s(s+1)} + \frac{12}{5} \frac{(s-1)}{(s-1)^2+1} + \frac{12}{5} \frac{-16/5}{(s-1)^2+1}$$

$$h(t) = \mathcal{L}^{-1}[H(s)] = \frac{-12}{5} e^{-t} + \frac{12}{5} e^t \cos(t) - \frac{4}{5} e^t \sin(t)$$

(b) $\frac{Y(s)}{X(s)} = \frac{4s-8}{(s+1)(s^2-2s+2)}$

For unit step $X(s) = \frac{1}{s}$

$$S(s) = \frac{Y(s)}{1/s} = \frac{4s-8}{(s+1)(s^2-2s+2)}$$

$$S(s) = \frac{4s-8}{(s)(s+1)(s^2-2s+2)}$$

$$S(s) = \frac{A}{s} + \frac{B}{s+1} + \frac{Cs+D}{s^2-2s+2}$$

$$4s - 8 = A(s+1)(s^2 - 2s + 2) + B(s)(s^2 - 2s + 2) + (C+D)(s)(s+1) \quad (20)$$

$$\boxed{s=0}$$

$$-8 = A(1)(2)$$

$$A = -4$$

$$\boxed{s=-1}$$

$$-12 = -B(1+2+2)$$

$$B = \frac{12}{5}$$

$$\boxed{s=1}$$

$$-4 = -4(2)(1-2+2) + \frac{12}{5}(1-2+2) + (C+D)(1)(2)$$

$$-4 = -8 + \frac{12}{5} + 2(C+D)$$

$$4 - \frac{12}{5} = 2(C+D)$$

$$\boxed{\frac{8}{10} = C+D}$$

 \Rightarrow

$$\boxed{D = \frac{8}{10} - C} \quad \text{--- (1)}$$

$$\boxed{s=2}$$

$$0 = -4(3)(4-4+2) + \frac{12}{5}(2)(4-4+2) + (2C+D)(6)$$

$$0 = -24 + \frac{48}{5} + (2C+D)6$$

$$24 - \frac{48}{5} = (2C+D)6$$

$$\frac{72}{5} = (2C+D)6$$

$$\frac{72}{30} = 2C+D$$

Part ①

21

$$\frac{F_2}{30} = 2C + \frac{8}{10} - C$$

$$\frac{F_2}{30} = \frac{10C + 8}{10}$$

$$\frac{F_2}{3} = 10C + 8$$

$$\frac{F_2 - 24}{30} = C$$

$$C = \frac{F_2 - 24}{30} = \frac{16}{10} = \frac{8}{5}$$

$$D = \frac{8}{10} - \frac{8}{5}$$

$$= \frac{-8}{10} = -\frac{4}{5}$$

$$S(s) = \frac{-4}{s} + \frac{12}{5(s+1)} + \frac{8s}{5(s^2-2s+2)} - \frac{4/5}{(s^2-2s+2)}$$

$$\mathcal{L}^{-1} S(s) = \mathcal{L}^{-1} \left[\frac{-4}{s} \right] + \mathcal{L}^{-1} \left[\frac{12}{5(s+1)} \right] + \frac{8}{5} \mathcal{L}^{-1} \left[\frac{s-1+1}{(s-1)^2+1} \right] - \frac{4/5}{5} \mathcal{L}^{-1} \left[\frac{1}{(s-1)^2+1} \right]$$

$$s(t) = \left(-4 + \frac{12}{5} e^{-t} + \frac{8}{5} e^t \cos t + \frac{4}{5} e^t \sin t \right) u(t)$$

$$\begin{aligned}
 \frac{d s(t)}{dt} &= -\frac{12e^{-t}}{5} + \frac{8e^t \cos t}{5} - \frac{8e^t \sin t}{5} + \frac{4e^t \sin t}{5} + \frac{4e^t \cos t}{5} \\
 &= -\frac{12e^{-t}}{5} + \frac{12e^t \cos t}{5} - \frac{4e^t \sin t}{5}
 \end{aligned}$$

Hence Verified